

Using scaling laws and hydraulic fracturing simulations to design and interpret block test experiments for future field extrapolation

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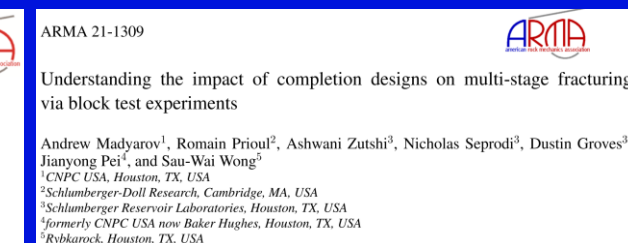
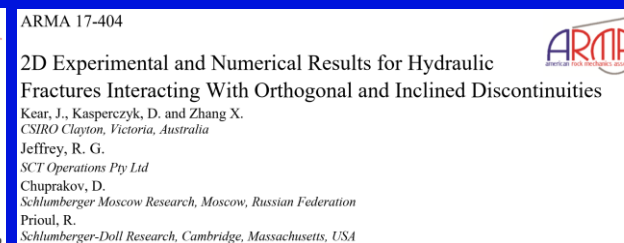
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Outline

1. Review of few key lab experiments
2. Scaling for point- and borehole-wellbore
3. Impact of completion design on multi-stage fracturing:
 - Design strategy
 - Experimental setup
 - Multi-cluster single stage experimental design and observations
 - Multi-perforation single-cluster experimental design and observations
4. Observations and discussions

Based on:

- 2017 ARMA Hydraulic Fracturing Workshop “On the role of laboratory experiments to validate hydraulic fracturing simulators”
- ARMA-2017-0404 on “2D Experimental and Numerical Results for Hydraulic Fractures Interacting With Orthogonal and Inclined Discontinuities”
- ARMA 21-1309 on “Understanding the Impact of Completion Designs on Multi-Stage Fracturing via Block Test Experiments”



Review of (some) key lab experiments over last 20 y

Increasing fracture and material complexity

- The importance of scaling hydraulic fracture experiments: lab \leftrightarrow field [1]
- Planar and non-planar fractures and artificial materials (PMMA, Glass, Cement):
 - Validation of tip asymptotics for fluid-driven cracks [CSIRO exp. + UMN] [2]
 - Hydraulic fracture height growth through stress contrasts [CSIRO exp. + SLB] [3,4]
 - Radial fracture initiation and propagation from a borehole [Delft + CSIRO exp. + SLB] [5]
 - Saucer-shaped (axi-symmetric) hydraulic fractures [CSIRO exp. + UMN] [6]
- Network of “planar” fractures and real rock materials (Sandstone, Limestone, Shale)
 - HF interacting with frictional discontinuities [Sandia, Delft, CSIRO, TerraTek exp.] [7,8]
 - HF interacting with discontinuities and laminated medium [TerraTek exp. + SLB] [9]
- 3D fractures in various materials (artificial and rock)
 - 3D fracture initiation and propagation [CSIRO and Delft]

More parameters to control and measure

[1] **Bunger, Jeffrey, and Detournay**, 2005. Application of Scaling Laws to Laboratory-Scale Hydraulic Fractures, 40th US Rock Mechanics Symposium, Alaska

[2] **Bunger and Detournay**, 2008. Experimental Validation of the Tip Asymptotics for a Fluid-Driven Fracture, Journal of the Mechanics and Physics of Solids, vol.56, no.11, pp. 3101-3115

[3] **Wu, Bunger, Jeffrey and Siebrits**, 2008. A comparison of numerical and experimental results of hydraulic fracture growth into a zone of lower confining stress, ARMA-08-267

[4] **Jeffrey and Bunger**, 2009. A detailed comparison of experimental and numerical data on hydraulic fracture height growth through stress contrasts. Soc. Pet. Eng. J., 14(3):413–422, 2009

[5] **Lecampion, Desroches, Jeffrey, Bunger**, 2016. Experiments versus theory for the initiation and propagation of radial hydraulic fractures in low permeability materials, JGR

[6] **Bunger, Gordeliy, and Detournay**, 2013. Comparison between laboratory experiments and coupled simulations of saucer-shaped hydraulic fractures in homogeneous brittle-elastic solids, J.Mech. Phys. Solids, 61(7):1636–1654

[7] **Chuprakov, Melchaeva and Prioul**, 2014, Injection-sensitive mechanics of hydraulic fracture interaction with discontinuities, Rock Mechanics Rock Engineering, 47 (5), 1625-1640.

[8] **Kear, Kasperczyk, Zhang, Jeffrey, Chuprakov, and Prioul**, 2017. 2D Experimental and Numerical Results for Hydraulic Fractures Interacting With Orthogonal and Inclined Discontinuities, ARMA 2017, San Francisco

[9] **Burghart, Desroches, Lecampion, Stanchits, Surdi, Whitney, Houston**, 2015, Laboratory study of the effect of well orientation, completion design, and rock fabric on near-wellbore hydraulic fracture geometry in shales, ISRM13

Review of (some) key lab experiments over last 20 y

Increasing fracture and material complexity

- The importance of scaling hydraulic fracture experiments: lab \leftrightarrow field [1]
- Planar and non-planar fractures and artificial materials (PMMA, Glass, Cement):

What we learned:

- ✓ Excellent match experiments-models
- ✓ Hydraulic fracturing mechanics theory works
- ✓ If material homogeneous and geometry of fracture known and simple

- Network of “planar” fractures and real rock materials (Sandstone, Limestone, Shale)

- ✓ Experiments and models matches partially or in some cases only
- ✓ Many parameters can't be measured and models are too simple

- 3D fractures in various materials (artificial and rock)

- ✓ No successful comparison experiment-model for 3D non-planar fractures

More parameters to control and measure

- [1] **Bunger, Jeffrey, and Detournay**, 2005. Application of Scaling Laws to Laboratory-Scale Hydraulic Fractures, 40th US Rock Mechanics Symposium, Alaska
- [2] **Bunger and Detournay**, 2008. Experimental Validation of the Tip Asymptotics for a Fluid-Driven Fracture, Journal of the Mechanics and Physics of Solids, vol.56, no.11, pp. 3101-3115
- [3] **Wu, Bunger, Jeffrey and Siebrits**, 2008. A comparison of numerical and experimental results of hydraulic fracture growth into a zone of lower confining stress, ARMA-08-267
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- [5] **Lecampion, Desroches, Jeffrey, Bunger**, 2016. Experiments versus theory for the initiation and propagation of radial hydraulic fractures in low permeability materials, JGR
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Application of Scaling Laws to Laboratory-Scale Hydraulic Fractures and validation of tip-asymptotics and HF regimes

- Energy dissipation during fluid-driven fractures (multi-scale tip asymptotics):

- Breaking material bond ahead of tip → Toughness-dominated regime (K) → LEFM
- Flow of viscous fluid → Viscosity-dominated regime (M, Desroches et al, 1994)

$$w \sim s^{1/2}$$

$$w \sim s^{2/3}$$

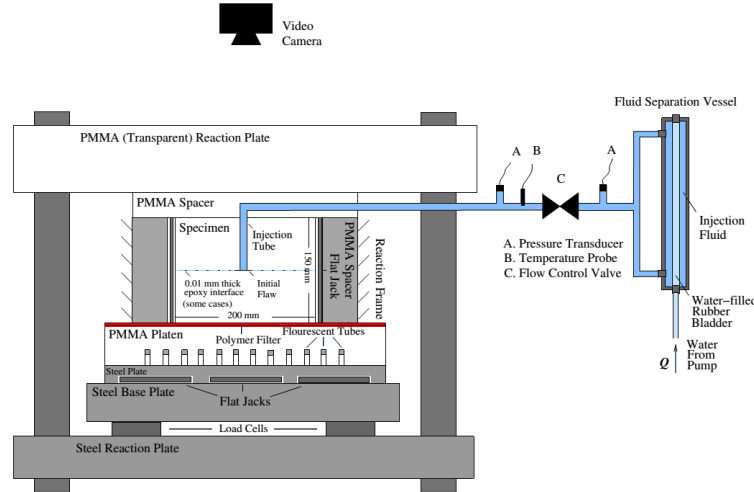
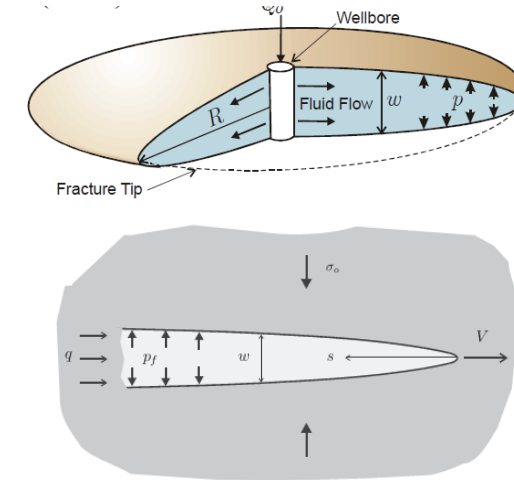
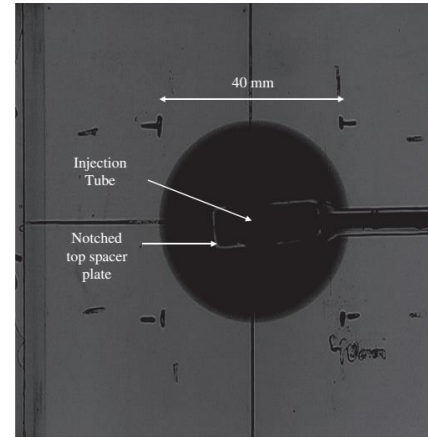
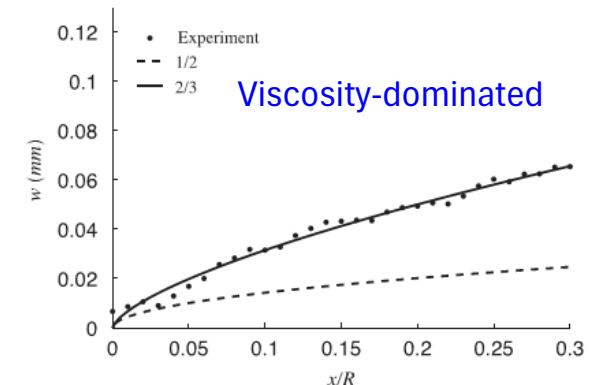
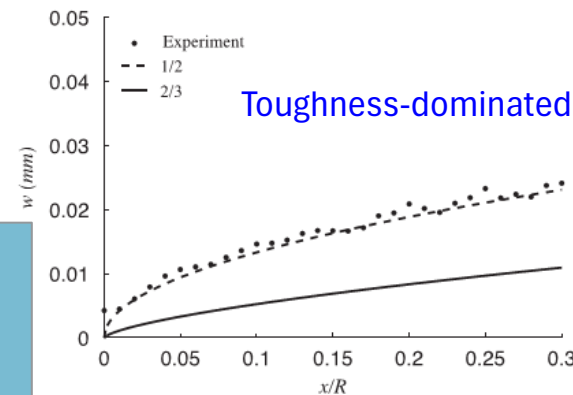


Fig. 3. Cross-sectional diagram of the setup for the laboratory experiments.



- Experiments in PMMA (8 exp) & Glass (3 exp) with glucose & glycerin
- Full-field crack opening measured using a photometric technique
- Known parameters: K_{IC} , E' , m , Q_0 , s_0

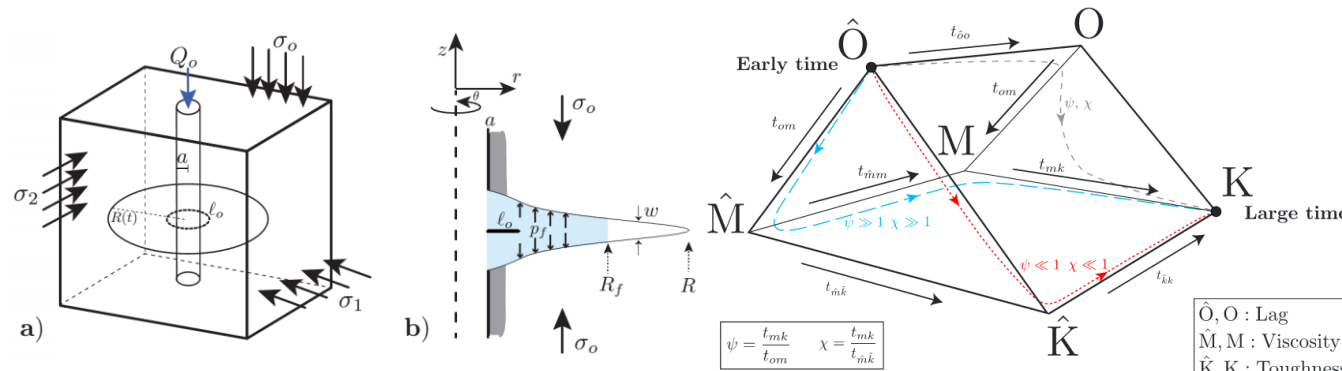
- ✓ HF mechanics theory works!
- ✓ Regime important to scale lab exp
- ✓ Other regimes: leakoff, lag...



Bunger, Jeffrey, and Detournay, 2005. Application of Scaling Laws to Laboratory-Scale Hydraulic Fractures, 40th US Rock Mechanics Symposium, Alaska

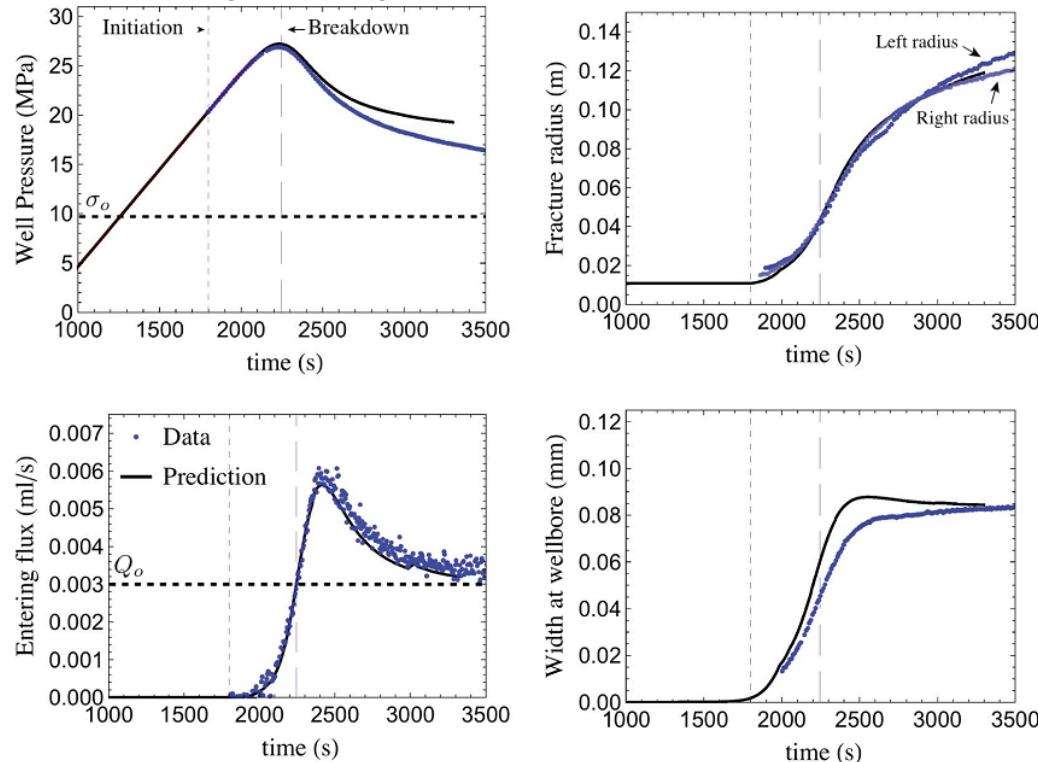
Bunger and Detournay, 2008. Experimental Validation of the Tip Asymptotics for a Fluid-Driven Fracture, Journal of the Mechanics and Physics of Solids, vol.56, no.11, pp. 3101-3115

Radial fracture initiation & propagation from borehole



- Early time: \hat{O} - \hat{M} - \hat{K} face
- Near-wellbore injection transient
- Fluid lag/compressibility dominated
- Late time: O - M - K face
- Constant injection rate propagation
- Toughness dominated

COV21c experiment (performed at TU Delft [De Pater et al., 1994])



- ✓ Initiation pressure \leq max pressure (aka breakdown):
 - Due to compressibility and viscosity/rate effects (observed Weijers, 1995, Zhao, 1995...)
- ✓ Breakdown pressure (a misnomer): related to injection transient
- ✓ HF mechanics works for simple geometry!
- ✓ We see again how important the fluid part is to understand the mechanics of HF

Dimensionless Parameters and Characteristic Timescales

- Radial fracture from a point source – most likely early-stage geometry (Bunger *et al.*, 2005)

- Viscosity $M = \left(\frac{t_m}{t}\right)^{2/5}$, $t_m = \left(\frac{\mu'^5 Q_o^3 E'^{13}}{K'^{18}}\right)^{1/2}$

- Stress/Lag $S = \left(\frac{t}{t_o}\right)^{1/5}$, $t_o = \frac{K'^6}{\sigma_o^5 E' Q_o}$

- Leak-off $C = \left(\frac{t}{t_c}\right)^{3/10}$, $t_c = \left(\frac{K'^4 Q_o}{C'^5 E'^4}\right)^{2/3}$

- Characteristic time for fracture radius to reach R_{\max} : $t_{\max} = \frac{R_{\max}^{5/2} K'}{Q_o E'}$

In the tight fields:

M – large: viscosity dominated

S – large: no lag, small $t_o \sim 10^{-4}$ s

C – small: little leak-off, Large $t_c \sim 10^6$ s

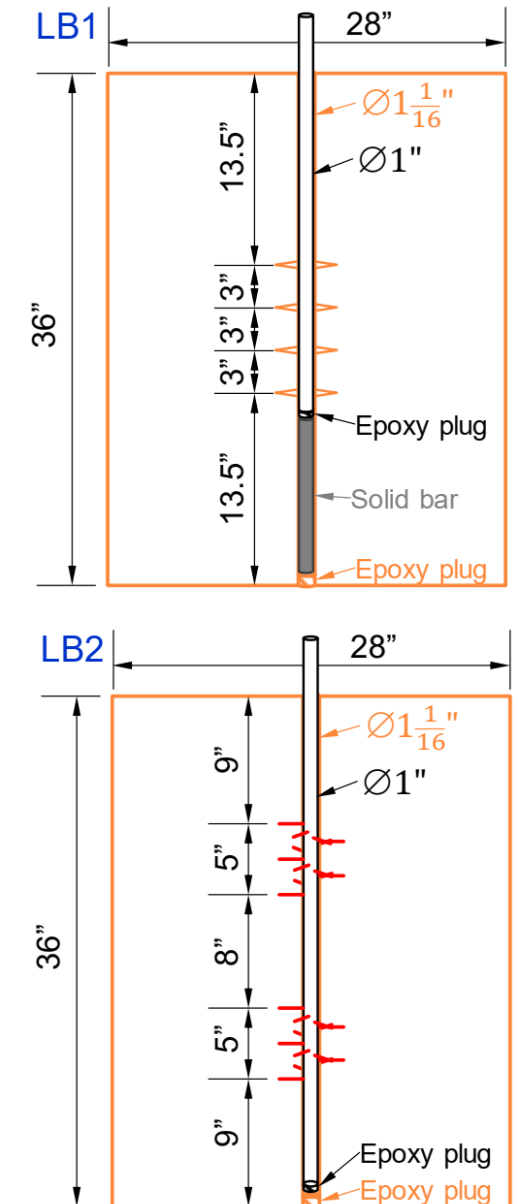
- Borehole source with compliance U (Lecampion *et al.*, 2017)

- Transient flow $t_{\text{lag}} = \frac{E'^2 \mu'}{\sigma_o^3}$, $t_U = \frac{E'^{5/2} U^{1/2} \mu'}{K'^3}$

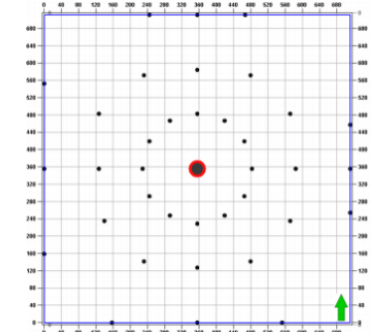
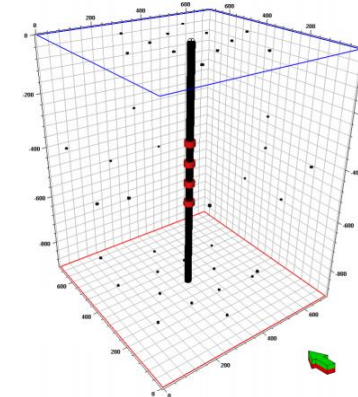
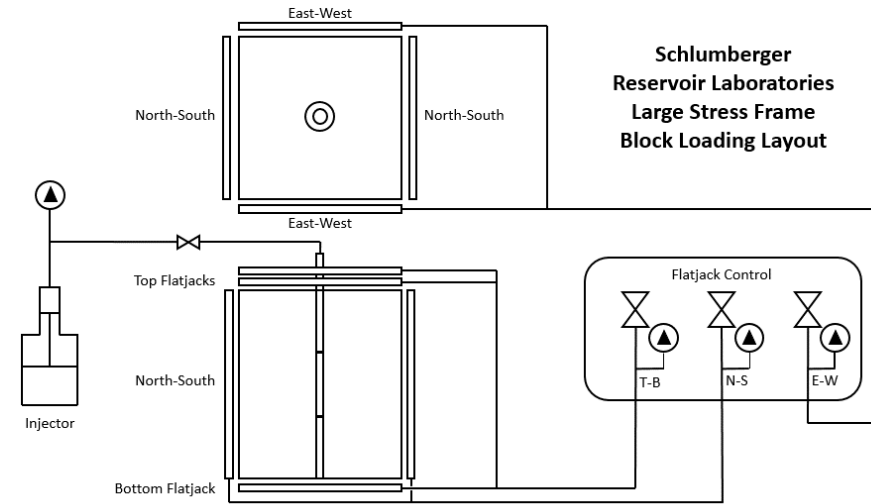
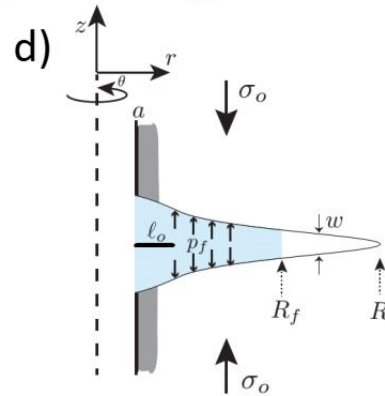
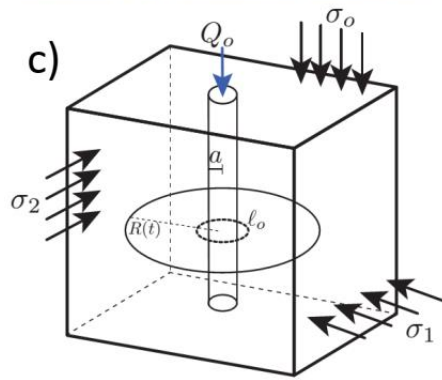
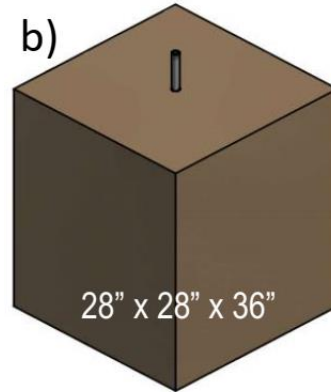
$$\psi = t_m / t_{\text{lag}}, \quad \chi = t_m / t_U$$

How to study impact of completion design on multi-stage fracturing in the lab for field purposes?

- **Initiation and propagation of multiple hydraulic fractures from perforation clusters in a single stage**
 - Simultaneous growth, cluster efficiency
 - Complex network vs. localized growth
 - Near-wellbore tortuosity
 - Effect of stage geometry, fluid rate, and viscosity
 - Effect of perforations
 - Interaction with bedding planes, joints, and natural fractures
- **Large Block hydraulic fracturing tests to study fracture patterns**
 - Far-field fracture geometry for **multi-cluster** one stage – LB1
 - Near-wellbore complexity from **individual perforations in a single cluster** – LB2



Experimental setup



	Field Scale	LB1	LB2
$E_H(\text{GPa})$	30	17.55	23.2
ν_H	0.22	0.24	0.22
$K_{Ic} (\text{MPa}\cdot\text{m}^{1/2})$	1.5-2.21	2.21	1.87
Porosity (%)		9.16	10.94
Permeability (mD)		0.1	0.443

- Polyaxial stress frame (sample $28 \times 28 \times 36''$)
- Three independent stresses applied by flatjacks, $\sigma_3' \leq \sigma_2' \leq \sigma_1' \leq 40 \text{ Mpa}$
- Wellbore fluid injection: viscosity $\mu = 1 - 2.5 \times 10^6 \text{ cp}$, rate $Q = 1 - 3,000 \text{ mL/min}$, pressure $p \leq 70 \text{ Mpa}$
- Acoustic emission monitoring (38 sensors)

Design of field-to-lab parameters using scaling analysis

- Balance between various physics – HF propagation regime:

- Lab experiment must reproduce propagation regime in the field using proper scaling of the parameters and test conditions need to be as close all possible to field conditions

- Scaling of stress conditions

$$(\sigma'_H/\sigma'_V)_{lab} = (\sigma'_H/\sigma'_V)_{field} \quad (\sigma'_h/\sigma'_V)_{lab} = (\sigma'_h/\sigma'_V)_{field}$$

$$R = (\sigma_H - \sigma_h)/(\sigma_V - \sigma_h) = 0.32$$

	Field Scale				Lab Scale			
σ_V	68	MPa	9863	psi	34	MPa	4931	psi
σ_H	51	MPa	7397	psi	19.55	MPa	2835	psi
σ_h	43	MPa	6237	psi	12.75	MPa	1849	psi
P_p	28	MPa	4061	psi	0	MPa	0	psi
σ'_V	40	MPa	5801	psi	34	MPa	4931	psi
σ'_H	23	MPa	3336	psi	19.55	MPa	2835	psi
σ'_h	15	MPa	2176	psi	12.75	MPa	1849	psi
R	0.32	-	0.32	-	0.32	-	0.32	-

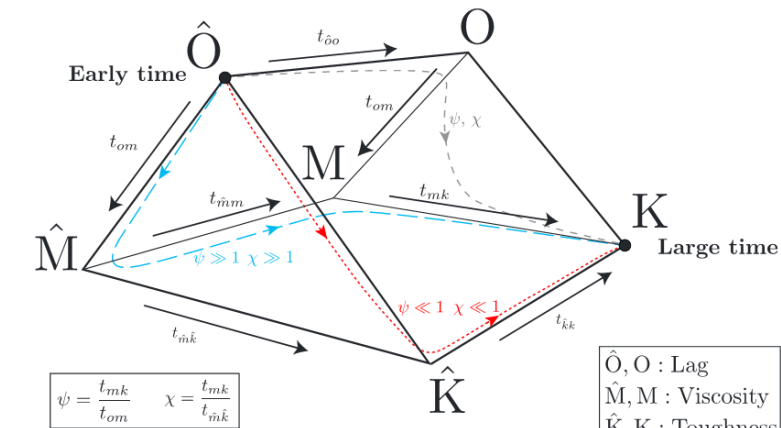
- Scaling of viscosity and injection rate - point-source:

- Matching dimensionless viscosity, M, between field and lab at characteristic “field” and “lab” propagation times (t_{field} and t_{lab}) leads to the viscosity-rate relation (lab viscosity ~1,000 times greater than field):

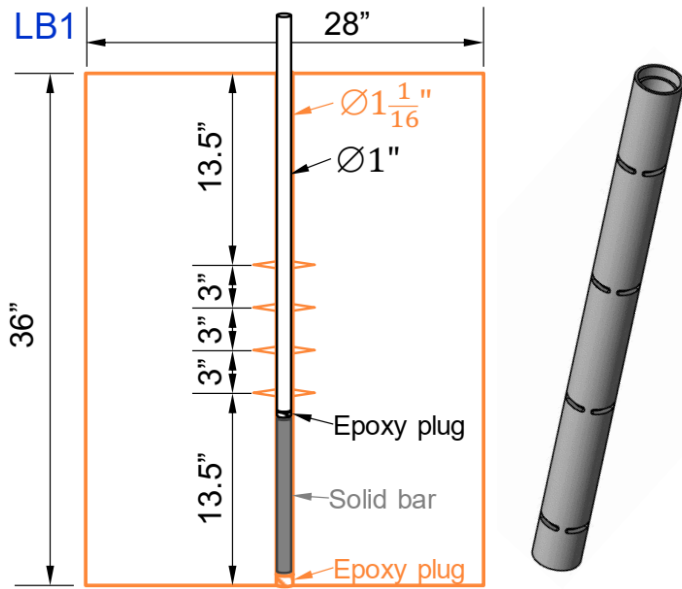
$$\mu_l Q_l = \mu_f Q_f \left(\frac{E'_f}{E'_l} \right)^3 \left(\frac{K_l}{K_f} \right)^4 \left(\frac{R_{lmax}}{R_{fmax}} \right) \quad t_{max} = \frac{R_{max}^{5/2} K'}{Q_o E'}$$

- Scaling of viscosity and injection rate: borehole-source

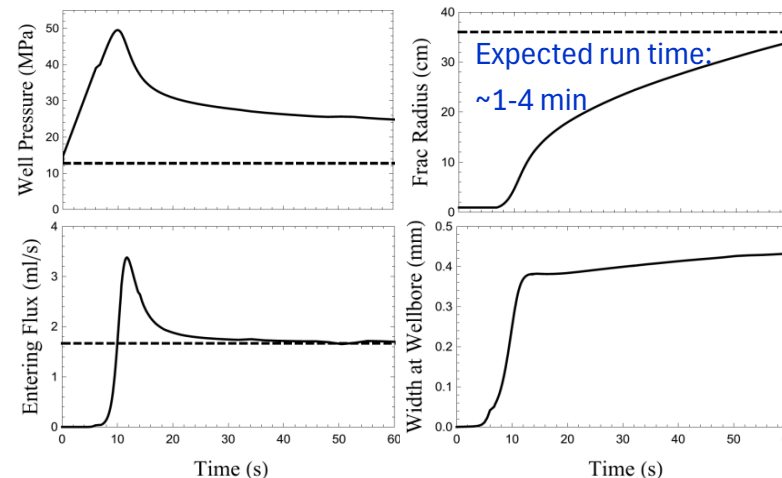
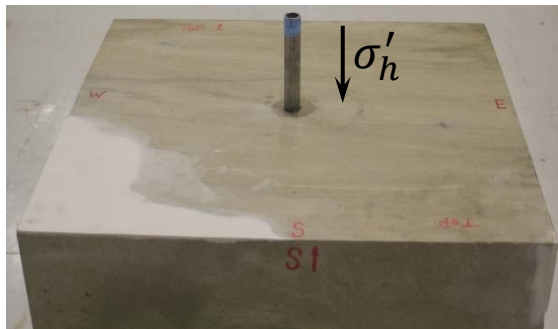
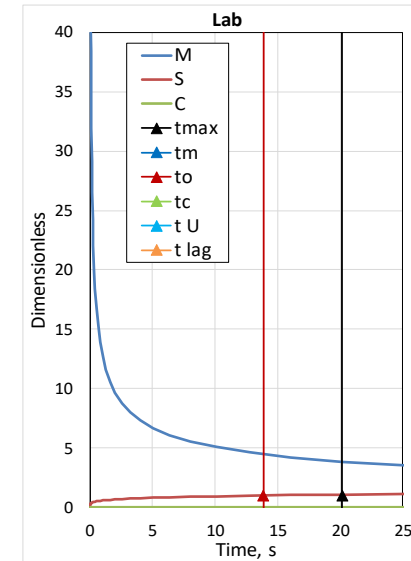
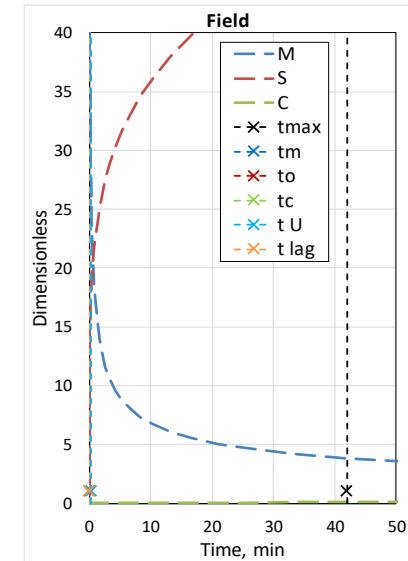
$$\psi \gg 1 \quad \chi \gg 1$$



LB-1 – multi-stage cluster



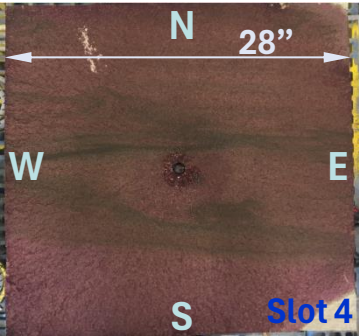
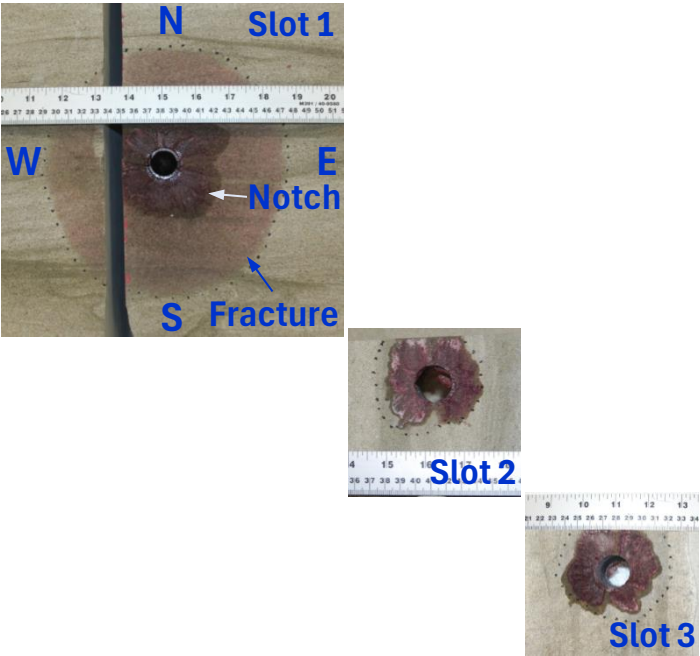
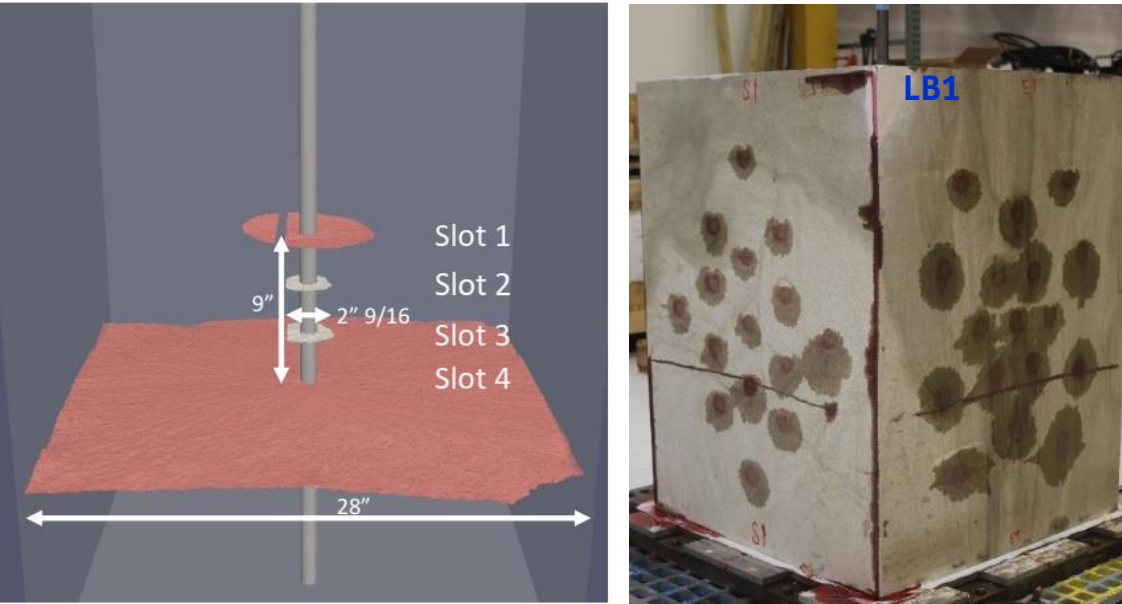
	Field scale		Lab scale LB1	
Propagation characteristics				
R_{max}	233 ~ 765	m ft	35.56 14	cm in
t_{max}	2,517 ~ 42	s min	20 1/3	s min
Fluid & Pumping				
Q	3 19	m^3/min bbl/min	85 5.3×10^{-4}	mL/min bbl/min
μ	25	cp	30,768	cp
U	1.67	m^3/GPa	0.41	mL/MPa
C_l	2.45×10^{-6}	m/\sqrt{s}	2.45×10^{-7}	m/\sqrt{s}
Characteristic dimensions				
Radius a	7.62	cm	1.35	cm
Notch l_o	30.48	cm	1.9	cm
	Field scale		Lab scale LB1	Unit
ψ	8.2×10^5		9.4	-
χ	3,689		18.3	-



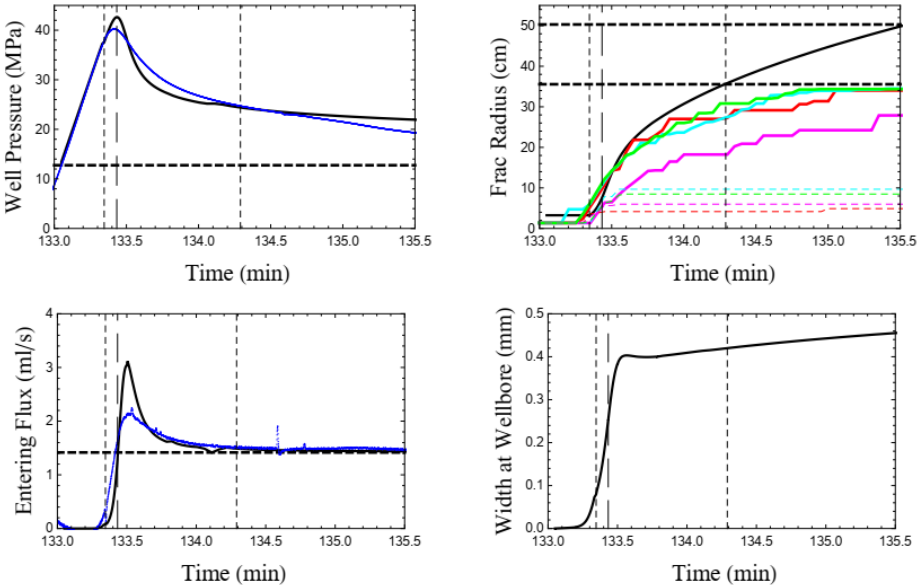
- Dimensionless viscosity M can be match between field and lab but S difficult to match

$$\psi \gg 1 \quad \chi \gg 1$$
- Q and μ needs to be chosen based on M matching and observation time
- HF simulation for one cluster very useful to give an indication of initiation/breakdown pressure, entering fluxes, width and observation time

LB-1 – Test Results

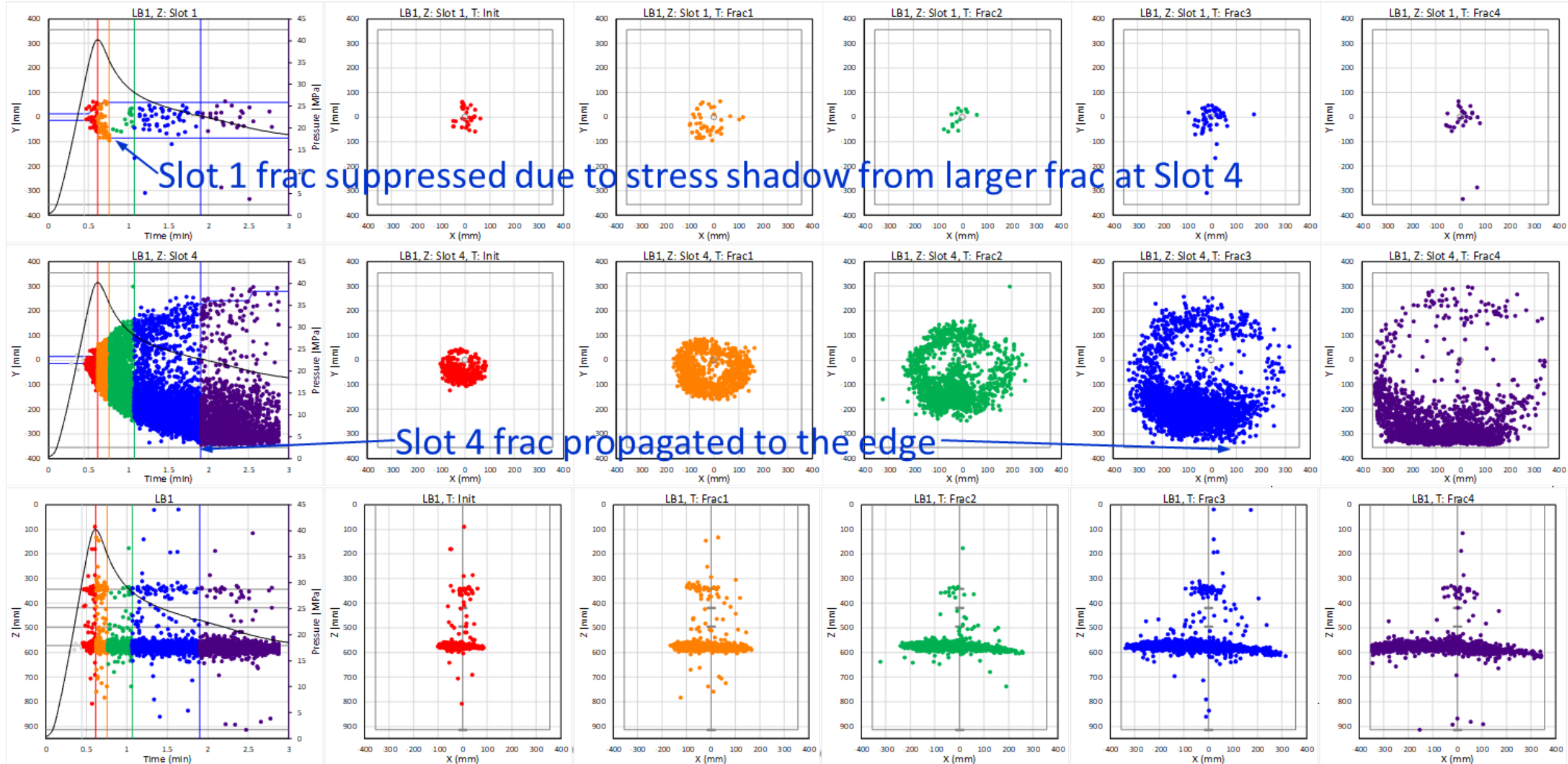


- Slot 1 frac ~ 4" radius
- Slots 2 & 3, fracs did not initiate
- Slot 4 frac ~ entire cross-section

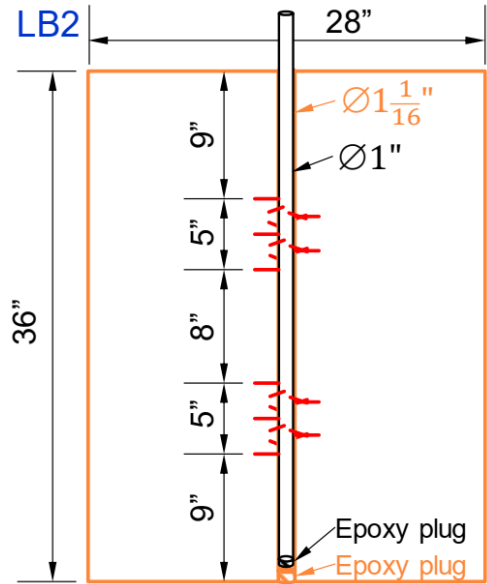


	Test	Model
Frac Initiation p_i , MPa	30.05	37.61
Breakdown p_b , MPa	40.23	42.64
Time: Init – Edge, s	87	55

LB-1 – Acoustic Emissions

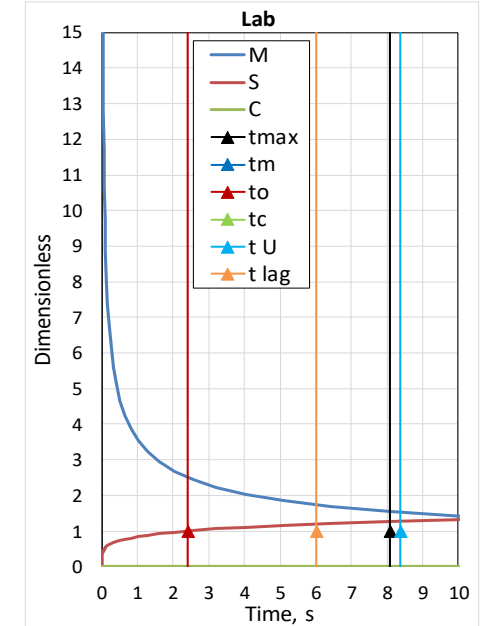
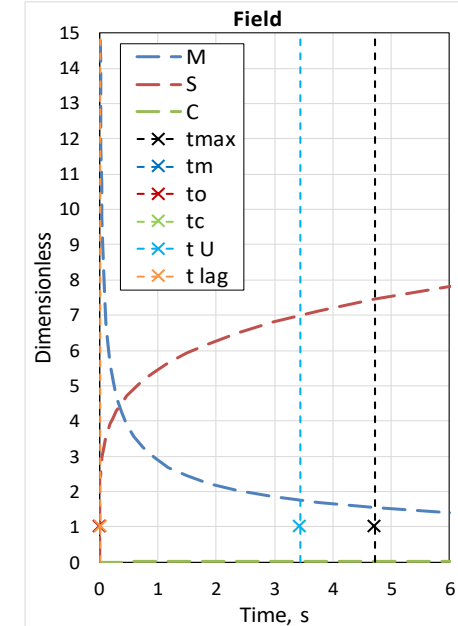


LB-2 – Individual perforations in a single cluster – 2 stages

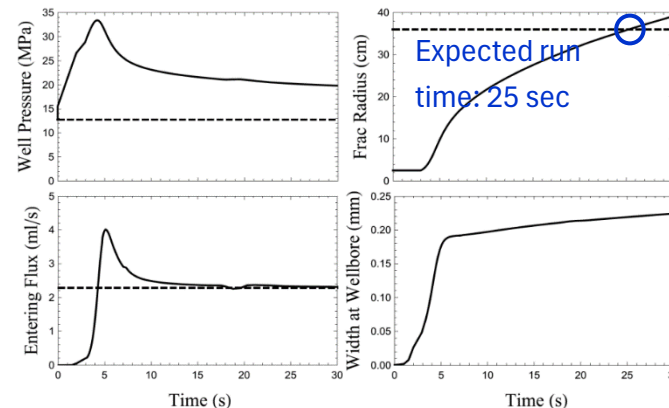


	Field scale		Lab scale LB2	
Propagation characteristics				
R_{max}	12.27	m	35.56	cm
	~ 40	ft	14	in
t_{max}^{top}	4.7	s	8	s
t_{bot}^{top}	9.4	s	16	s
Fluid & Pumping				
Q^{top}	1.5	m^3/min	137	mL/min
Q^{bot}	0.75	m^3/min	69	mL/min
μ^{top}	5	cp	1,758	cp
μ^{bot}	5	cp	1,745	cp
U	13	m^3/GPa	0.41	mL/MPa
C_l	2.45×10^{-6}	m/\sqrt{s}	2.45×10^{-7}	m/\sqrt{s}
Characteristic dimensions				
Radius a	7.62	cm	1.35	cm
Perf depth l_p	30.48	cm	2.54	cm
	Field scale		Lab scale LB2	
Q	1.5	0.75	137	69
	m^3/min	m^3/min	mL/min	mL/min
ψ	796	281	4	1.4
χ	4.1	1.45	4.1	1.45

LB2 Top Stage Design



- 2 stages with different injection rates
- 13 Perforations (60° phased) per stage, sand-jetted through holes in casing
- Packer system to isolate stages



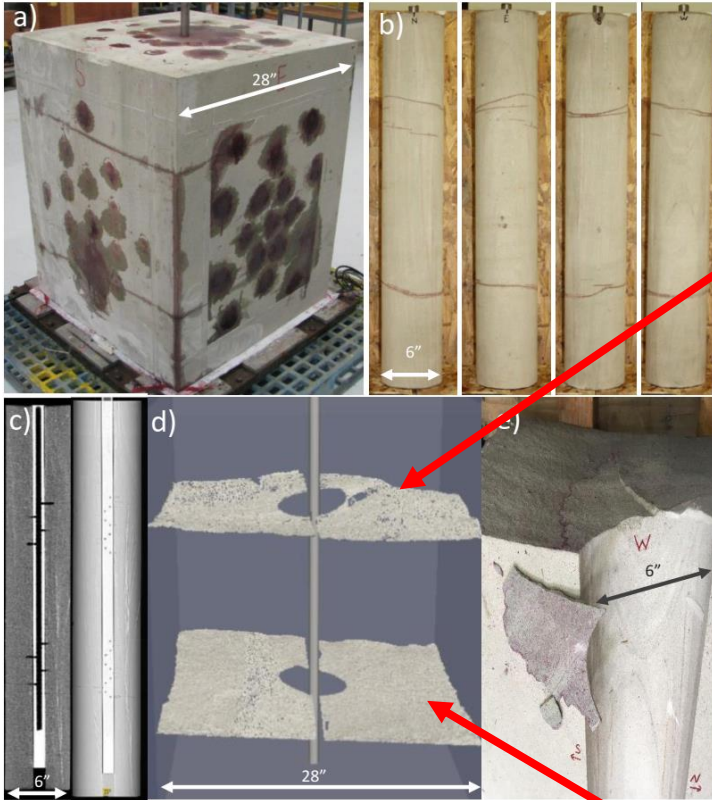
- Dimensionless viscosity M can be match

$$\chi_f^{top} = \chi_l^{top} = 4.1 \quad \psi > 1$$

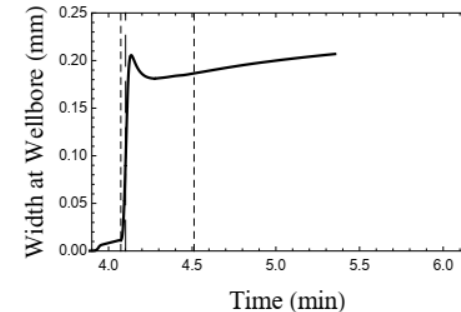
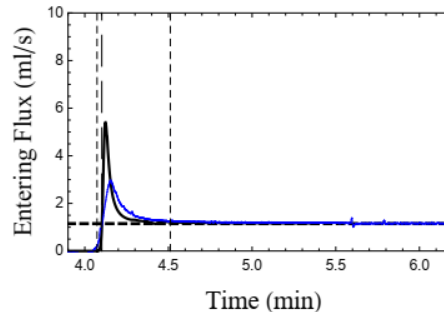
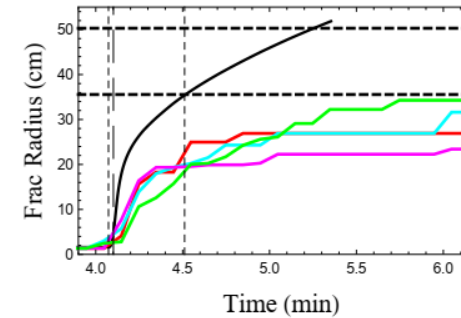
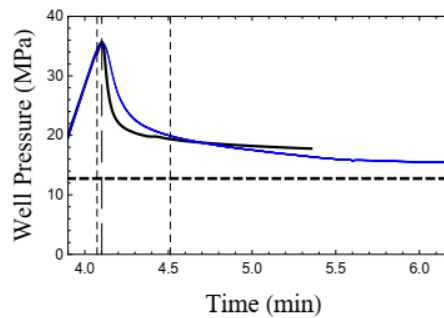
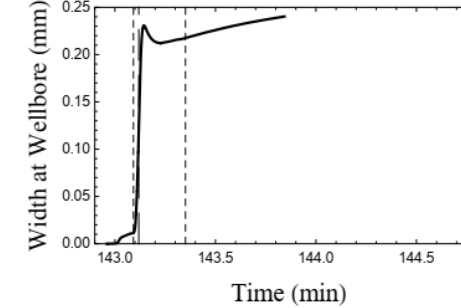
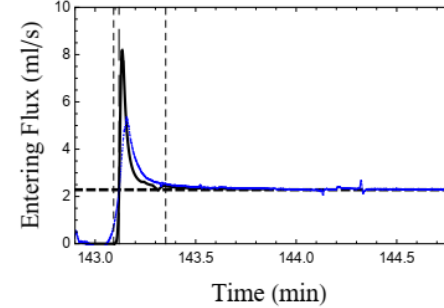
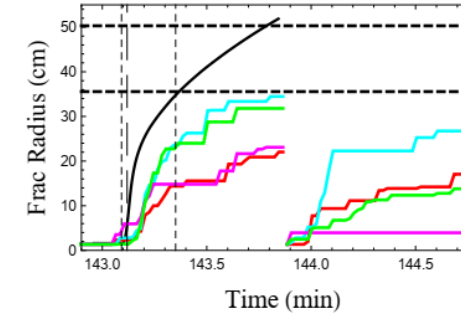
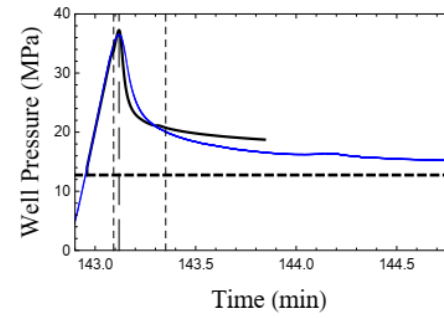
$$\chi_f^{bot} = \chi_l^{bot} = 1.45$$

- Initiation/breakdown pressure, entering fluxes, width and observation time much more difficult to estimate prior to experiment with single radial fracture simulator given completion design

LB-2 – Test Results



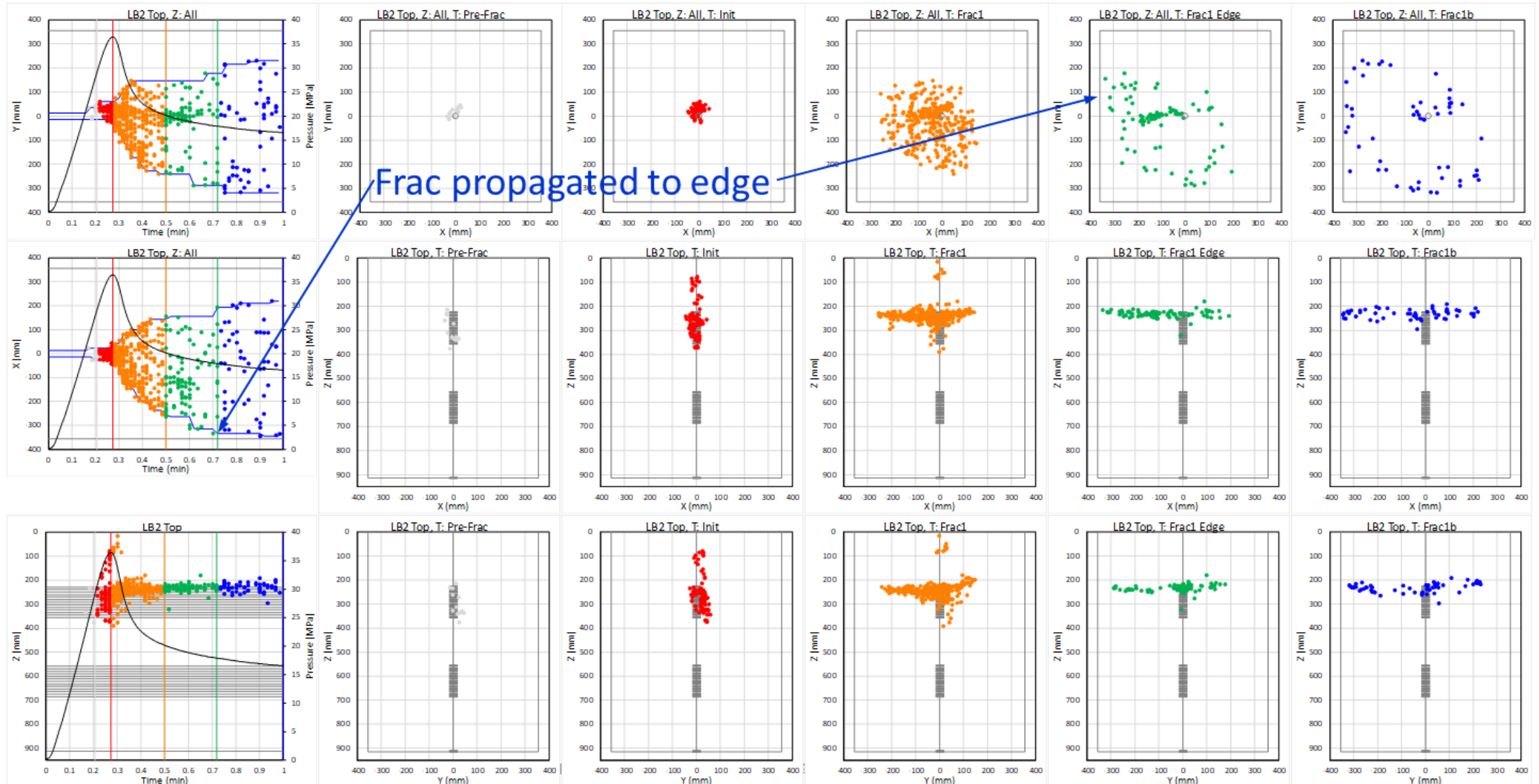
- One fracture reached block faces at each stage
- “Petal” fractures at individual perforations join into a twisted frac
- Fractures merge at Top stage



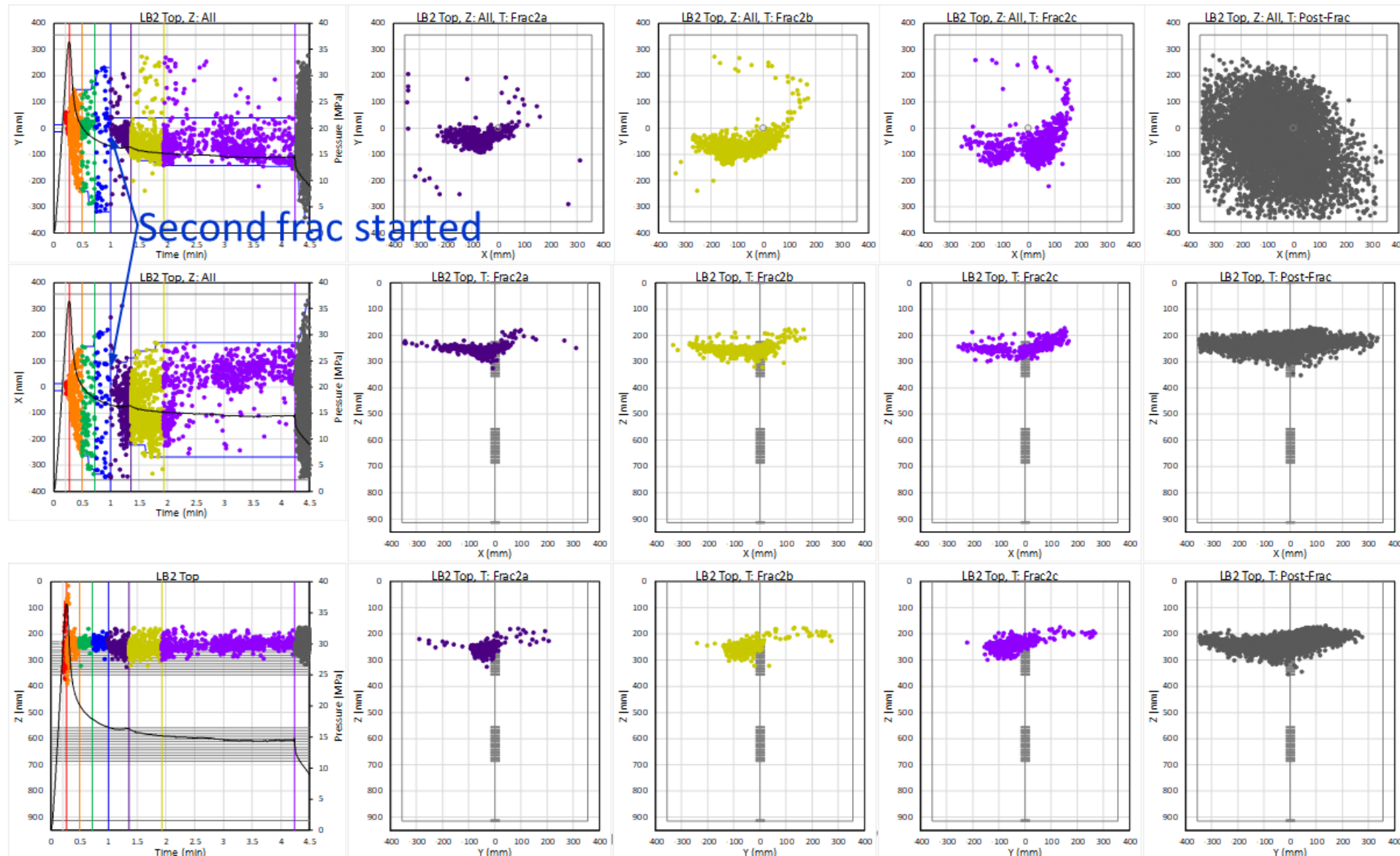
LB2 Top	Test	Model
Frac Initiation p_i , MPa	29.12	33.77
Breakdown p_b , MPa	36.46	37.26
Time: Init – Edge, s	31	16.5

LB2 Bottom	Test	Model
Frac Initiation p_i , MPa	31.8	33.76
Breakdown p_b , MPa	35.48	35.68
Time: Init – Edge, s	90	27.6

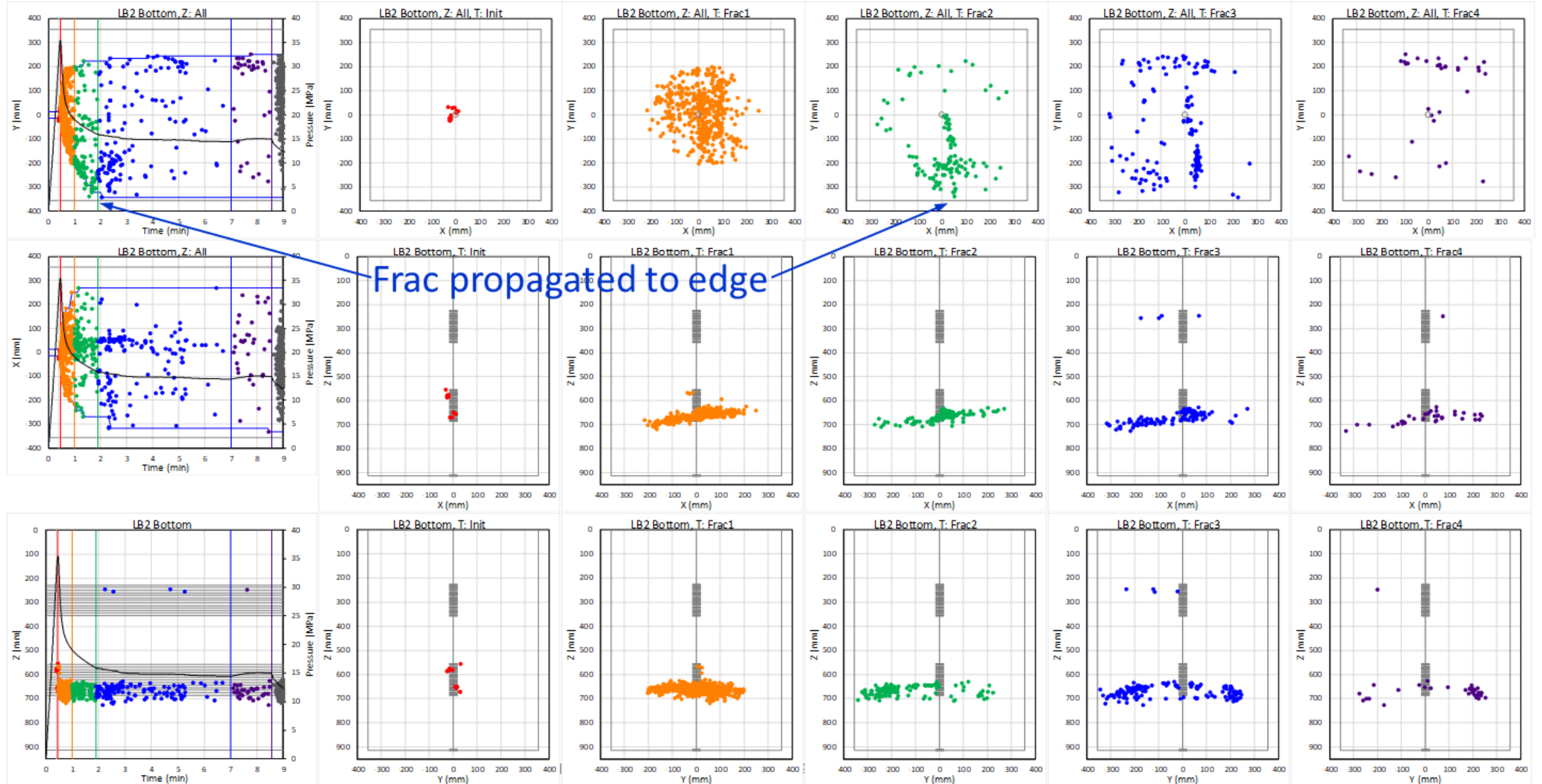
LB-2 Top – Acoustic Emissions: First Fracture



LB-2 Top – Acoustic Emissions: Second fracture



LB-2 Bottom – Acoustic Emissions



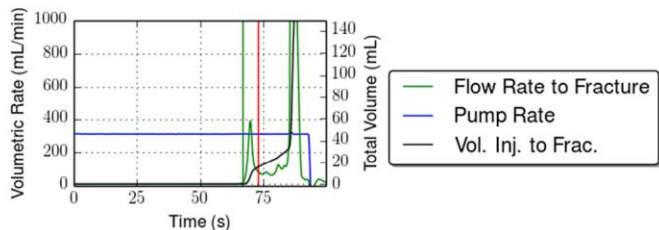
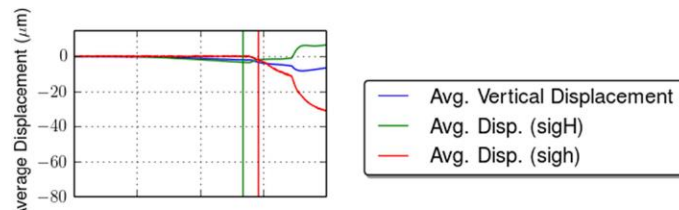
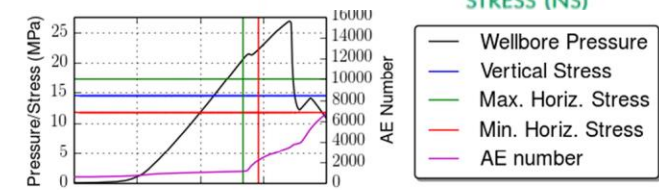
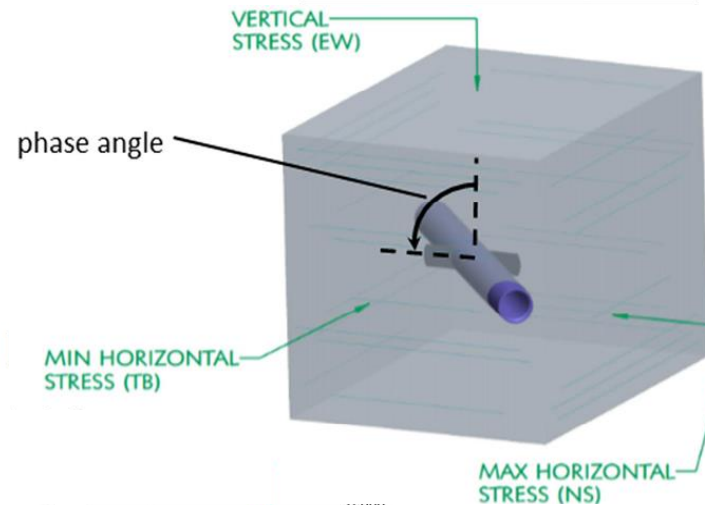
Observations on LB-1 and LB-2 block experiments



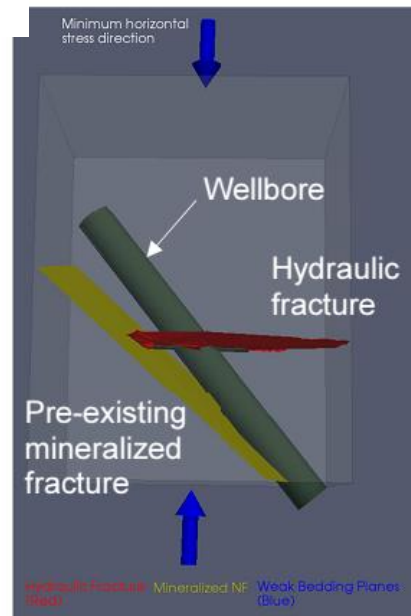
1. **LB1 – far field design: one stage with 4 slots**
 - Cluster efficiency: only two clusters activated but one fracture dominated, maybe due to stress shadow or unbalanced fluid partitioning into one fracture (?)
2. **LB2 – near-wellbore design: two single-cluster stages with different injection rate**
 - Complex initiation, increasing with injection rate (counter-intuitive)
 - Near-wellbore complexity limited to 2-3 perf lengths
 - Top stage: primary fracture with near-wellbore tortuosity, then second fracture once first one reached the end of the block
3. **Observations on design:**
 - Field-to-lab scaling to match viscosity dominated conditions easy to do with scaling relationship but not easy to match all M, S, and C parameters at the same time
 - Borehole-source parameters more difficult to match but possible
 - HF simulator for single radial fracture very useful to define rate and viscosity and assess observation time, initiation and breakdown pressure
 - Acoustic emissions most useful for interpretation of time-evolving geometry
 - Difficult to control “limited entry friction” akin to field conditions

HF interacting with many discontinuities/laminations

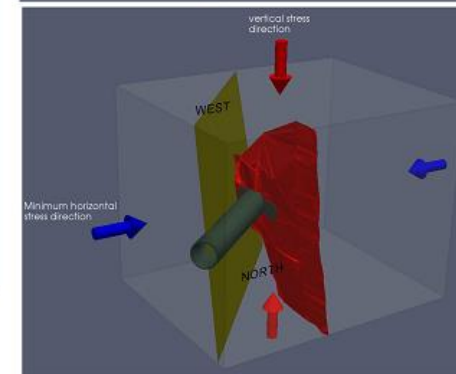
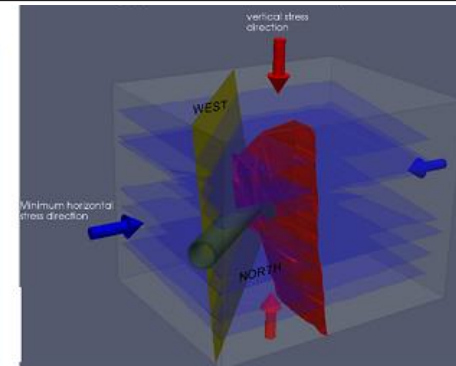
Niobrara shales



Parameter	Typical field treatment	Laboratory
Wellbore diameter (mm)	133	89
Pumping rate (m ³ /s)	0.01325	5.1×10^{-6}
Fluid viscosity (Pa-s)	0.01	0.1
Plane strain modulus (GPa)	28.7	28.7
Toughness (Pa-√m)	1.5×10^6	1.5×10^6
Wellbore storage compressibility (m ³ /Pa)	2.3×10^{-8}	8.9×10^{-12}

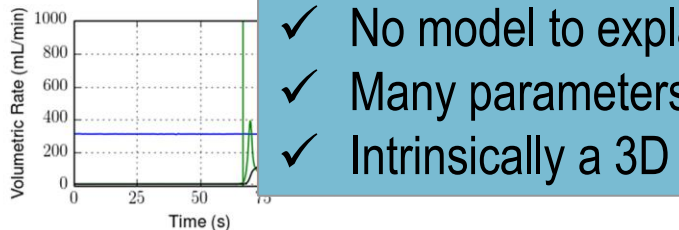
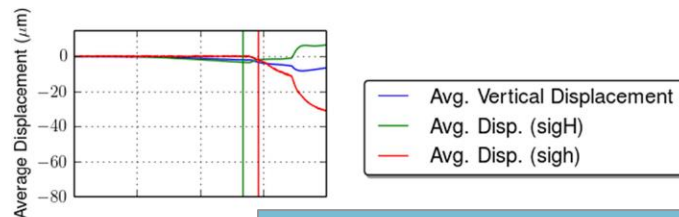
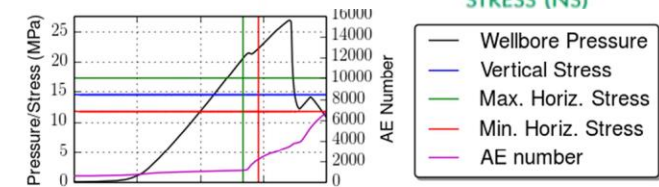
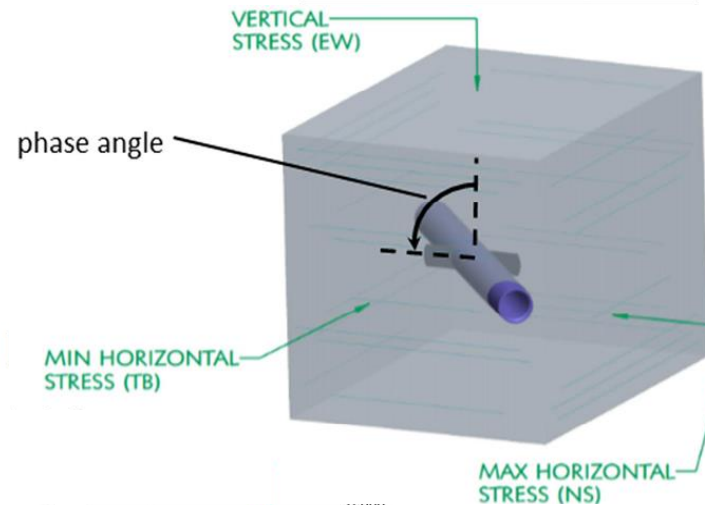


Top view

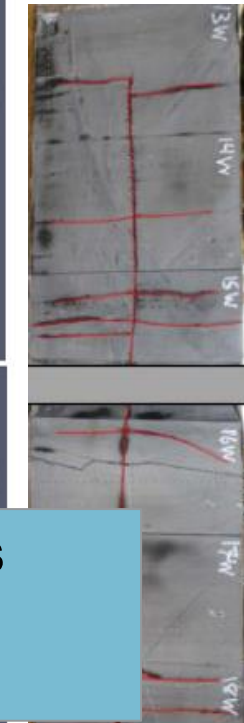
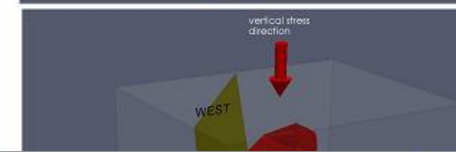
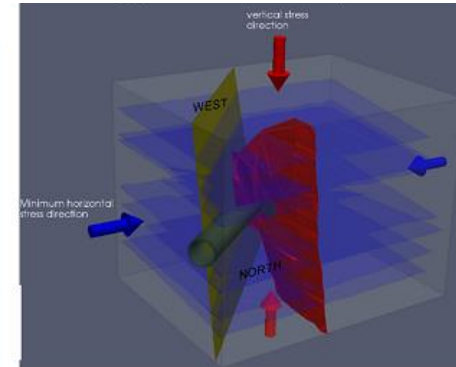
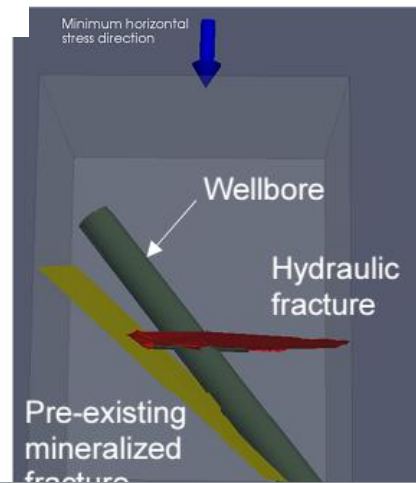


HF interacting with many discontinuities/laminations

Niobrara shales



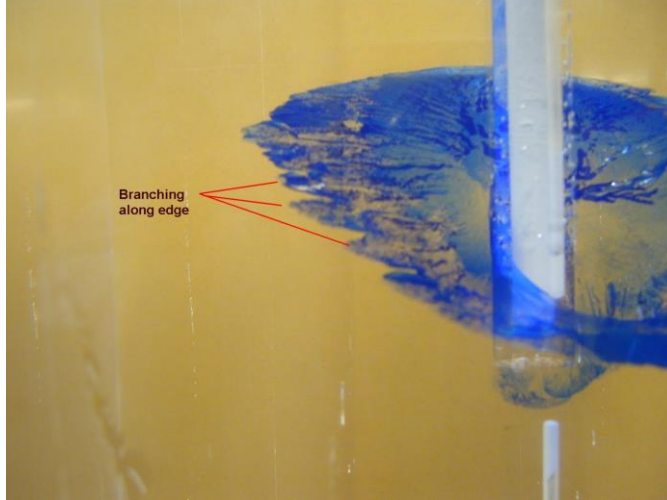
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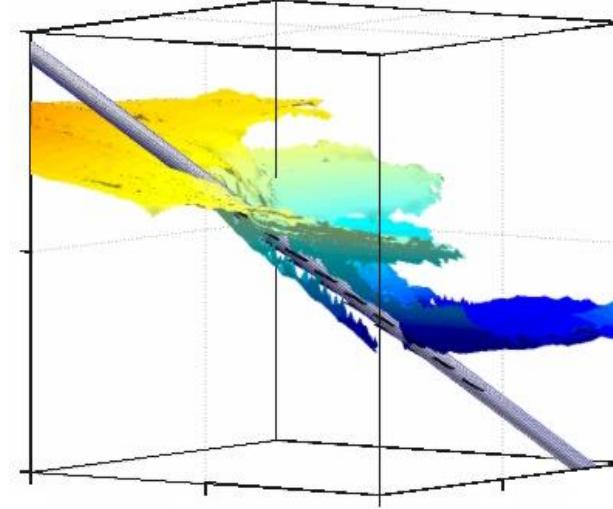
- ✓ No model to explain the experiments with NF and many laminations
- ✓ Many parameters can't be measured
- ✓ Intrinsically a 3D problem

3D hydraulic fracture initiation and propagation

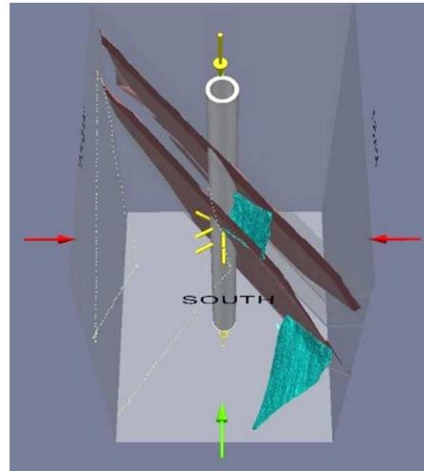
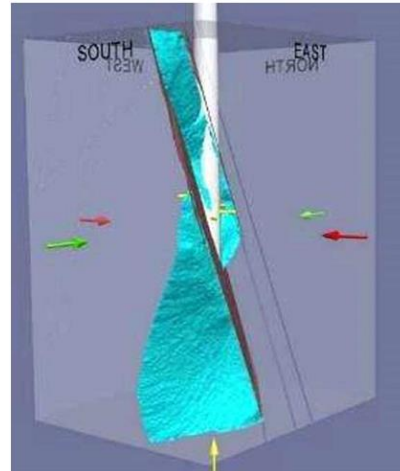
CSIRO experiment



Delft Fracturing Consortium, 1997



URTeC 2460449



✓ No successful comparison experiment-model for 3D non-planar fractures (mode I, II, III)?

Discussion points

- Tremendous lab experiment progresses over the last 20 years: Hydraulic fracturing mechanics theory works!
- Excellent match experiments-models if material homogeneous and geometry of fracture known and simple
- Scaling laws and simple HF simulator essential to design lab experiments to match field conditions for “viscosity” regime
- Hard to match all the far-field and near-wellbore dimensionless quantities: trade-off necessary on focused goals

What’s missing:

- We do a good job from Field-to-Lab, less obvious to translate learnings from Lab-to-Field? Seems easier with fluid experiments (proppant, fibers), not so when rock and fracturing involved
- Limited-entry conditions difficult to reproduce in the lab: what is a simple criteria to achieve conditions akin to the field?
- We need new “simple” dimensionless quantities for more complex cases
- Increasing fracture and material complexity means increasing number of parameters: necessary evil or a dead-end? Is there another way?
- How do we address the heterogeneity and multiscale nature of HF in the lab with real rocks? Linking the lab and field scales?
- What are the key missing experiments to validate numerical simulators?

